

In[65]:= **f = x + y + 1 / (x * (y + 1) ^ 2)**

Out[65]= $x + y + \frac{1}{x (1 + y)^2}$

In[66]:= **gradijent = D[f, {{x, y}}]**

Out[66]= $\left\{ 1 - \frac{1}{x^2 (1 + y)^2}, 1 - \frac{2}{x (1 + y)^3} \right\}$

In[67]:= **Tacke = Solve[gradijent == 0, {x, y}]**

Out[67]= $\left\{ \left\{ x \rightarrow -\frac{1}{\sqrt{2}}, y \rightarrow -1 - \sqrt{2} \right\}, \left\{ x \rightarrow -\frac{i}{\sqrt{2}}, y \rightarrow -1 - i \sqrt{2} \right\}, \right.$
 $\left. \left\{ x \rightarrow \frac{i}{\sqrt{2}}, y \rightarrow -1 + i \sqrt{2} \right\}, \left\{ x \rightarrow \frac{1}{\sqrt{2}}, y \rightarrow -1 + \sqrt{2} \right\} \right\}$

In[68]:= **Hodf = Simplify[D[f, {{x, y}, 2}]**

Out[68]= $\left\{ \left\{ \frac{2}{x^3 (1 + y)^2}, \frac{2}{x^2 (1 + y)^3} \right\}, \left\{ \frac{2}{x^2 (1 + y)^3}, \frac{6}{x (1 + y)^4} \right\} \right\}$

In[69]:= **HodfM = MatrixForm[Hodf]**

Out[69]//MatrixForm=

$$\begin{pmatrix} \frac{2}{x^3 (1+y)^2} & \frac{2}{x^2 (1+y)^3} \\ \frac{2}{x^2 (1+y)^3} & \frac{6}{x (1+y)^4} \end{pmatrix}$$

In[70]:= **HodfuTacke = Hodf /. Tacke**

Out[70]= $\left\{ \left\{ \left\{ -2 \sqrt{2}, -\sqrt{2} \right\}, \left\{ -\sqrt{2}, -\frac{3}{\sqrt{2}} \right\} \right\}, \left\{ \left\{ 2 i \sqrt{2}, i \sqrt{2} \right\}, \left\{ i \sqrt{2}, \frac{3 i}{\sqrt{2}} \right\} \right\}, \right.$
 $\left. \left\{ \left\{ -2 i \sqrt{2}, -i \sqrt{2} \right\}, \left\{ -i \sqrt{2}, -\frac{3 i}{\sqrt{2}} \right\} \right\}, \left\{ \left\{ 2 \sqrt{2}, \sqrt{2} \right\}, \left\{ \sqrt{2}, \frac{3}{\sqrt{2}} \right\} \right\} \right\}$

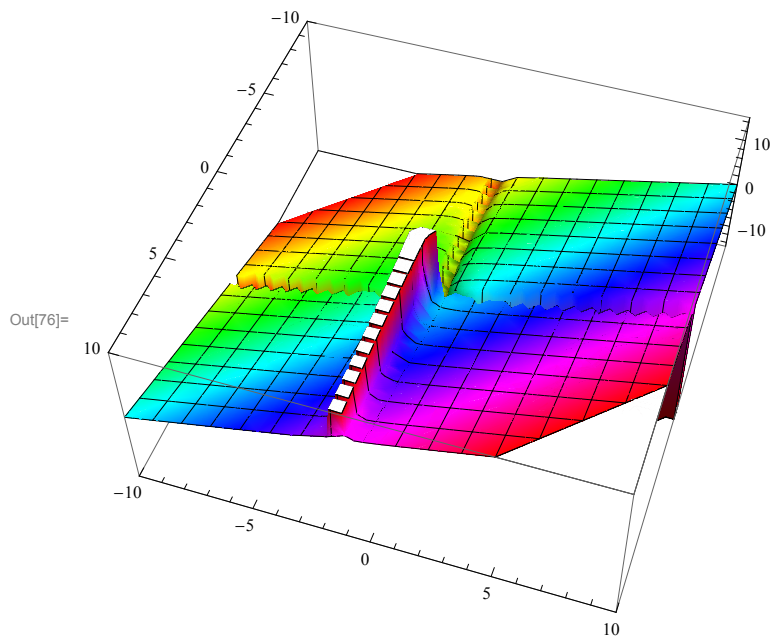
In[71]:= **minf = Map[PositiveDefiniteMatrixQ, HodfuTacke, 1]**

Out[71]= {False, False, False, True}

In[72]:= **maxf = Map[PositiveDefiniteMatrixQ, -HodfuTacke, 1]**

Out[72]= {True, False, False, False}

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In[76]:= Plot3D[f, {x, -10, 10}, {y, -10, 10}, ColorFunction -> Hue,  
PlotRange -> {{-10, 10}, {-10, 10}, {-15, 15}}]
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In[77]:= Show[%76, ImageSize -> Full]
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